

Introduction to Nonlinear Control

Errata for the First Edition

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This document contains a list of errata for the first edition of [Introduction to Nonlinear Control: Stability, Control Design, and Estimation](#) published by Princeton University Press. Please email Philipp Braun (philipp.braun@anu.edu.au) if you discover additional errors, and the errors will be included in future updates.

- (page 77), before Equation (3.44): “feasiblity” needs to be “feasibility”.
- (page 77), below Equation (3.45): “ $V(x) = z(x)Pz(x)$ ” needs to be “ $V(x) = z(x)^\top Pz(x)$ ”.
- (page 107), Equation (4.28): Equation (4.28) needs to be changed from

$$P = -\frac{1}{2\pi j} \oint_{\Gamma} \frac{G'_{ol}(s)G_{ol}(s)k}{1 + G_{ol}(s)G_{ol}(s)k} ds \quad \text{to} \quad P = -\frac{1}{2\pi j} \oint_{\Gamma} \frac{G'_{ol}(s)k}{1 + G_{ol}(s)k} ds$$

- (page 133), Definition 6.4: The role of y_0 can be made more precise by clarifying that it is a condition on the initial condition $y_0 = Cx_0 \in \Omega$ of the system (6.8).
- (page 140) Equation (6.30): In Equation (6.30) a bracket is missing. It should be $\frac{r_1}{r_2} \text{Re}(\cos(\theta_1 - \theta_2) + j \sin(\theta_1 - \theta_2))$ instead of $\frac{r_1}{r_2} \text{Re}(\cos(\theta_1 - \theta_2) + j \sin(\theta_1 - \theta_2))$.
- (page 146) Estimate of $\dot{V}(x)$: In the derivation of an estimate for $\dot{V}(x)$ on page 146, the term $-\varepsilon x^T(A^T P + PA)x$ needs to be replaced by $x^T(A^T P + PA)x$. In particular, the derivations should read

$$\begin{aligned} \dot{V}(x) &= x^T(A^T P + PA)x - 2x^T P b \psi(y) + 2\eta \beta \psi(y) c \dot{x} \\ &= x^T(A^T P + PA)x - 2x^T P b \psi(y) + 2\eta \beta \psi(y) c (Ax - b \psi(y)) \\ &\leq x^T(A^T P + PA)x - 2x^T P b \psi(y) \\ &\quad + 2\eta \beta \psi(y) c (Ax - b \psi(y)) - 2\psi(y)(\psi(y) - \beta y) \\ &= x^T(A^T P + PA)x - 2x^T (Pb - \eta \beta A^T c^T - \beta c^T) \psi(y) \\ &\quad - 2(\eta \beta c b + 1) \psi(y)^2 \\ &= x^T(A^T P + PA)x - 2x^T (Pb - \hat{c}^T) \psi(y) - 2d \psi(y)^2. \end{aligned}$$

- (page 184): The expressions $\text{sign}(dz(u)) = \text{sign}(\text{sat}(u))$ and $\text{sign}(q) = \text{sign}(u - q)$ need to be replaced by $\text{sign}(dz(u)) \text{sign}(\text{sat}(u)) \geq 0$ and $\text{sign}(q) \text{sign}(u - q) \geq 0$, respectively. The original expression are not necessarily correct in the case that $\text{sign}(\cdot)$ is equal to zero.
- (page 187): In Equation (8.38) and in Equation (8.40), the term “ $-Lq$ ” needs to be replaced by “ $+Lq$ ” (four times).
- (Page 190) below Equation (8.51): “ $x \in \mathbb{R}^{n_u}$ ” needs to be replaced by “ $x \in \mathbb{R}^n$ ”.
- (page 191): In the expression before Equation (8.53) the term “ $-Lq$ ” needs to be replaced by “ $+Lq$ ”.
- (page 194) Equation (8.64): The term “ $(Gw + Kx + Lq - q)$ ” needs to be replaced by “ $(Gw + Kx + Lq - q + Hx)$ ”, i.e., the term $+Hx$ is missing.
- (pages 197-198): In the matrix between Equation (8.70) and Equation (8.71), “ D ” needs to be replaced by “ DW^{-1} ”. In Equations (8.71), (8.72) and in the Matrix after Equation (8.72), “ D ” needs to be replaced with “ $D\Lambda_2$ ”.

- (page 205): The equality

$$\dot{V}(x) = L_f V(x) + L_g V(x)k(x) + \frac{1}{2} (L_g V(x))^2 + \frac{1}{2} w^2,$$

needs to be replaced with the inequality

$$\dot{V}(x) \leq L_f V(x) + L_g V(x)k(x) + \frac{1}{2} (L_g V(x))^2 + \frac{1}{2} w^2.$$

- (page 309) Theorem 13.2: The matrix C needs to satisfy $C \in \mathbb{R}^{p \times n}$ instead of $C \in \mathbb{R}^{p \times m}$.
- (page 335) Theorem 14.10: The matrix defined in (14.37) needs to be Schur (not Hurwitz).
- (page 471): In the first estimate of $\dot{V}(e_x)$ the expression “ $(\bar{P}^T e_x)$ ” needs to be replaced by “ $(\bar{P}^T e_x)^T$ ”.